Homework 2

Due: Start of class, September 14th

- 1. Griffiths Problem 1.55 (4th Edition; called 1.54 in the 3rd Edition) **[4pts]** Hints: $(\cos(x))^2 = \frac{1}{2}\cos(2x) + \frac{1}{2}and (\sin(x))^2 = \frac{1}{2} - \frac{1}{2}\cos(2x)$.
- Griffiths Problem 2.2 (only part (b) of the 3rd Edition) [2pts] *Hints:* Use visual symmetry to determine which field component(s) is/are non-zero.
- 3. Griffiths Problem 2.6 **[4pts]** *Hints:* Remember u-substitution; consider $u = s^2 + z^2$.
- Griffiths Problem 2.12 [3pts]
 Hints: The problem is referring to the integral form of Gauss's Law.
- 5. Griffiths Problem 2.18 **[2pts]** *Hints:* Look at Griffiths's hint and recall superposition.
- 6. Griffiths Problem 2.21 [3pts]

Hints: Since $r \to \infty$ is your reference point, the integral to find the potential inside of the sphere is best broken up into two integrals, one from ∞ to *R* and the other from *R* to *r*. Note that you found the field for the inner region in Griffiths Problem 2.12.

7. Griffiths Problem 2.28 [3pts]

Hints: The law of cosines (i.e. the more general form of the Pythagorean theorem) can be used to find the length of the side of a triangle given two side lengths and the angle that is opposite to the side of interest: $c^2 = a^2 + b^2 - 2ab \cos \theta_c$. This can be used to get the distance between a point within a sphere to some point outside, e.g. on the z-axis. Do the integrals in order φ , θ , r and employ u-substitution for the θ integral. It turns out $\frac{1}{rz} \left(\sqrt{r^2 + z^2 + 2rz} - \sqrt{r^2 + z^2 - 2rz} \right) = \frac{2}{z} for r < z$ and $\frac{2}{r} for r > z$.