Tuesday March 31

See the [course webpage](#) for slides, video links, and google docs Q&A links

Topics for this Lecture:

- *Angular momentum*

$$F_{applied} = kx$$ spring force

$F_{applied} = k{*}x = F_{gravity} = mg$ spring scale

***Exam 2 will be through circular motion**

***The exam window will be 30 hrs, but you will only have a 1-hour to complete the exam once you start**

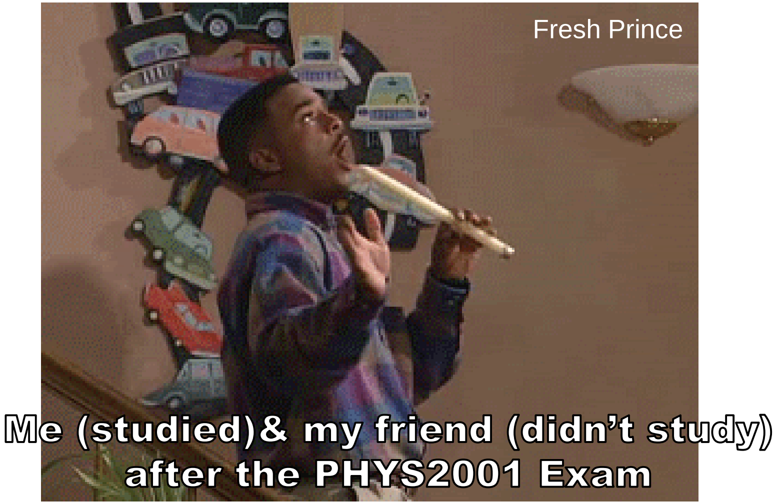
***If your internet fizzles mid-exam, contact me or Dr. Piccard as soon as possible afterward.**

****If your circumstances hinder your completion of any of this class's assignments, please let me know***

***These slides are recorded in advance for your convenience. Administrative details may be out of date. Keep an eye on your email please.**

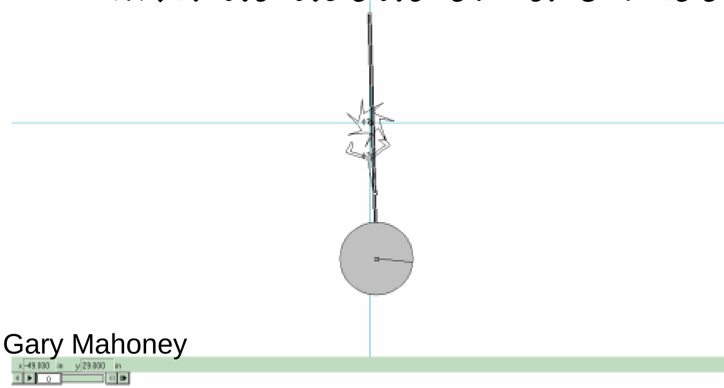
- Assignment 10 due Friday
- Pre-class due 15min before 1:30pm Tue/Th
- Help Room: via Teams, 6-9pm Wed/Thurs, also via email on Wed/Thurs
- SI: via Teams
- Office Hours: via email (meisel@ohio.edu)
- Midterm 2: Open from Noon April 6 through 6pm April 7, but only 60min to complete once started. (Less traffic expected Late Monday & on Tuesday).

Set aside time to study!



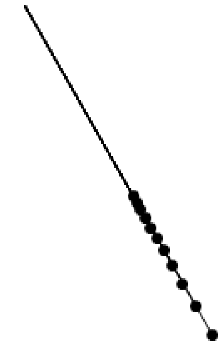
Simple Harmonic Motion

What length pendulum should I choose to make a clock that ticks once per second? ...what about on the moon?



Gary Mahoney

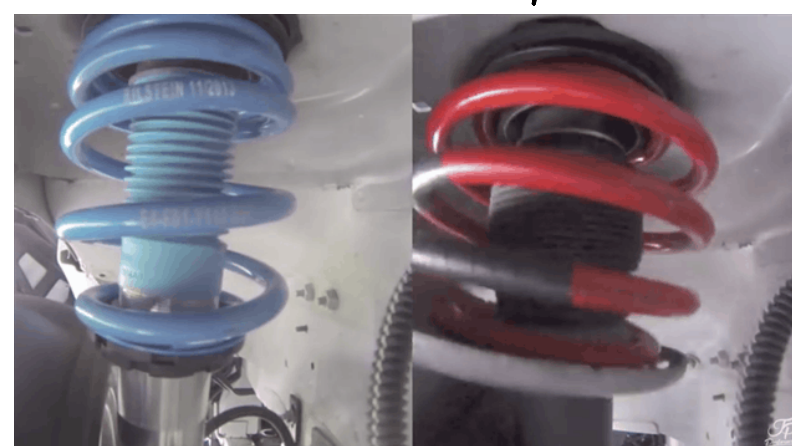
How do I predict when these pendula of different lengths will re-align?



Sol Lederman

Why did this happen at Tacoma Narrows?

How do you select a spring for a race car vs sedan suspension?



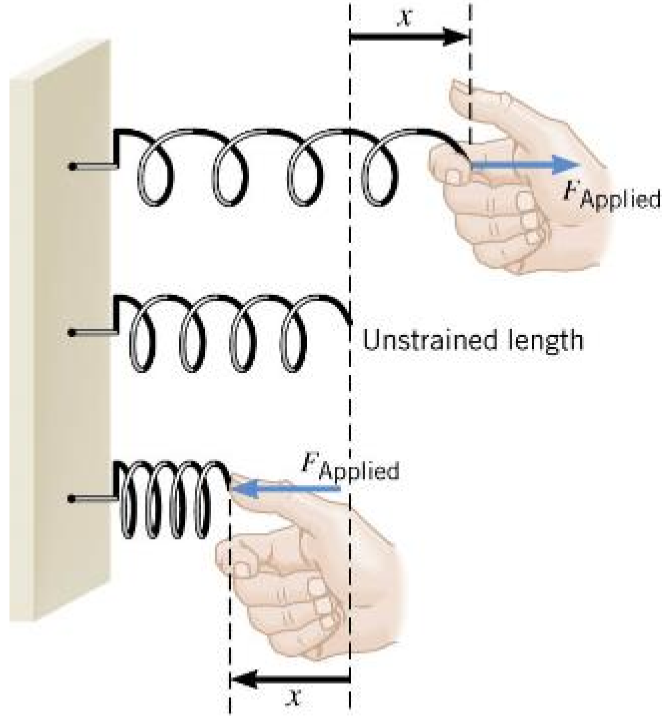
What are the units for the spring constant, k?

A. N
B. m/N
C. N*m
D. N/m
E. kg*m
F. kg*N

1. Spring constant, k = F/x. F= force applied, x = displacement of spring.
2. SI units for F: N
3. SI units for x: m
4. SI units for k: N/m

Springs: Hooke's Law 📖 Sect 16.1

- The displacement of a stretchy-object (e.g. spring) from it's equilibrium position (where it is when you're not touching it) requires a force linearly proportional a property of the spring, k.
  - **$F_{applied}$ = k*x**
  - F = applied force
  - x = displacement
  - k = spring constant (SI units: N/m)
- This is "Hooke's Law"

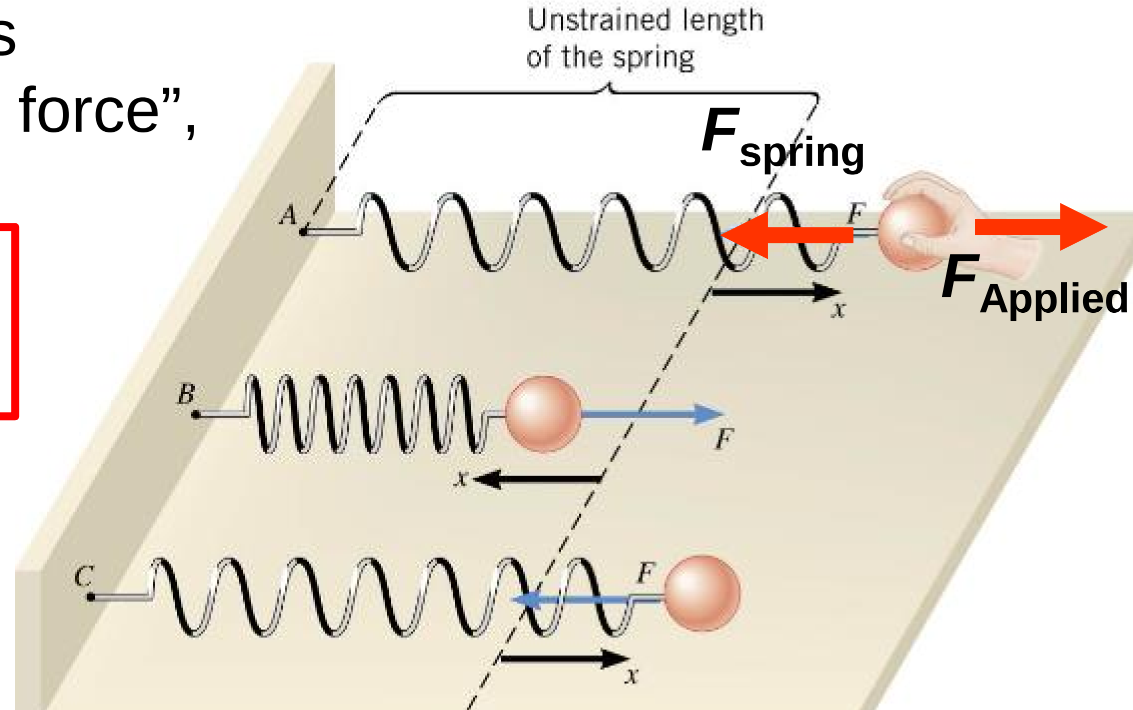


Cutnell & Johnson, Physics, 6th ed, Fig. 10.1

*The sign of x depends on the direction of displacement!
You choose which way is +x & the other way is -x.

Springs: Applied Force & Restoring Force

- The force you apply to stretch (or compress) a spring is balanced by a "restoring force", a.k.a. the spring force.
  - $F_{applied} = -F_{spring} = k*x$
  - $F_{spring} = -k*x$

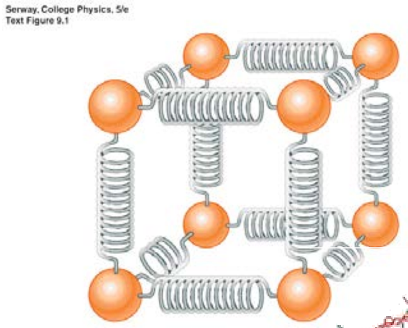


Cutnell & Johnson, Physics, 6th ed, Fig. 10.1

Springs: Anything that stretches & tries to return to equilibrium!

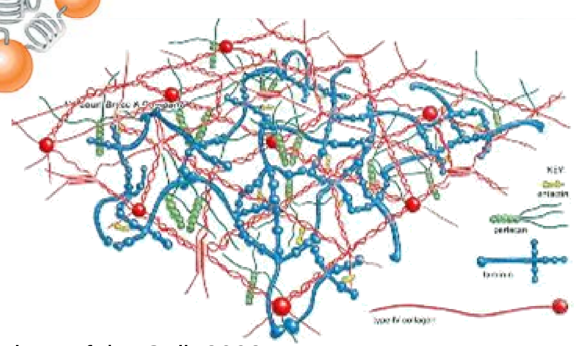
- Hooke's law applies to anything with "elasticity"
  - I.e. objects which can stretch & tend to return to the position from which they were stretched
  - E.g. Springs, rubber bands, taught guitar strings, bridges in the wind, etc.

- Complicated solids held together by molecular bonds are well represented by coupled spring systems.



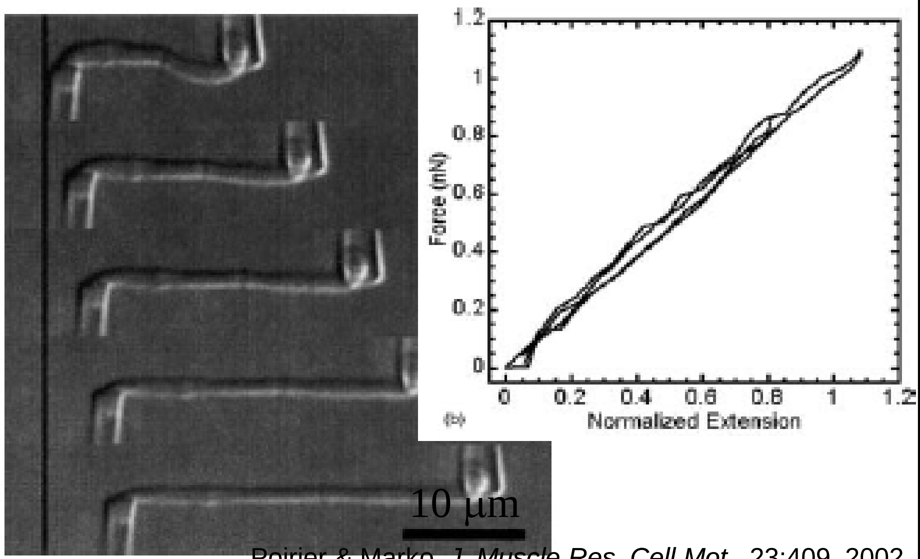
Extracellular Matrix

(the framework that supports cells)



Alberts et al, Molecular Biology of the Cell, 2002

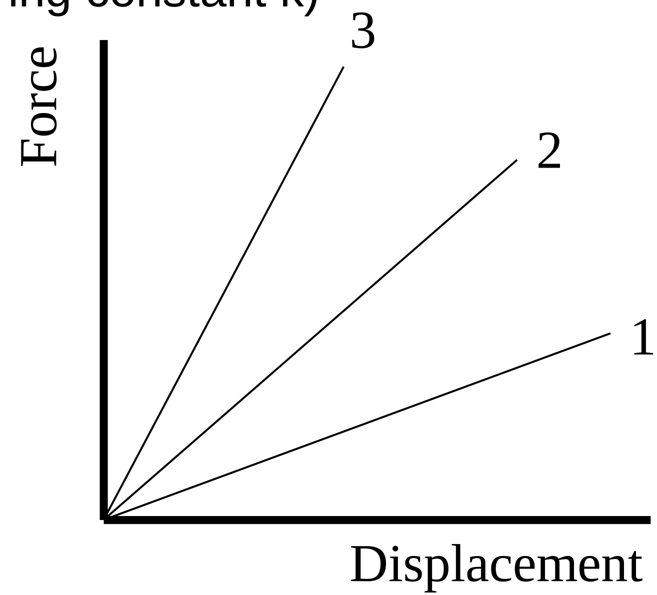
Newt Chromosome: $F=k*x$



Poirier & Marko, *J. Muscle Res. Cell Mot.*, 23:409, 2002

This graph represents the behavior of three springs.
Which one is the "stiffest"? (i.e. has the largest spring constant k)

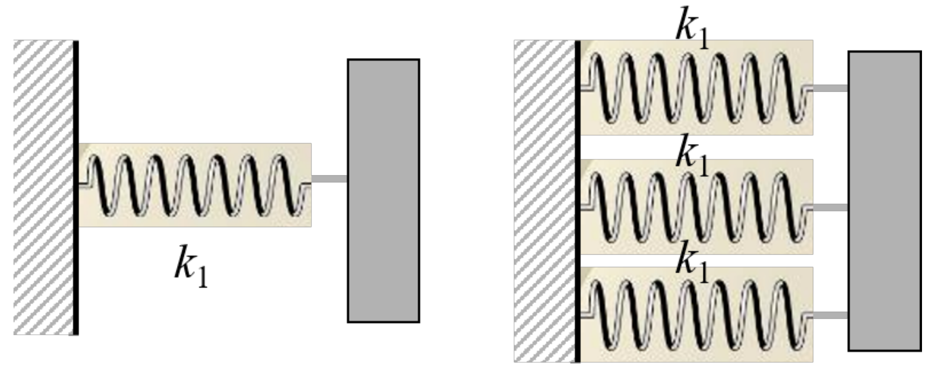
A. 1
B. 2
C. 3
D. All the same



1. "Stiffness" indicates how large a spring constant is.
2. "Stiff" = large k.
3. F = k*x
4. k = F/x
5. The slope of F vs x gives k.
6. Spring 3 has the largest slope, therefore the largest k, and so is the stiffest.

Suppose you attach a mass to three identical springs and stretch them by 1cm. If you attached the same mass to one spring and displaced it by 1cm, how much force would the single spring require in comparison?

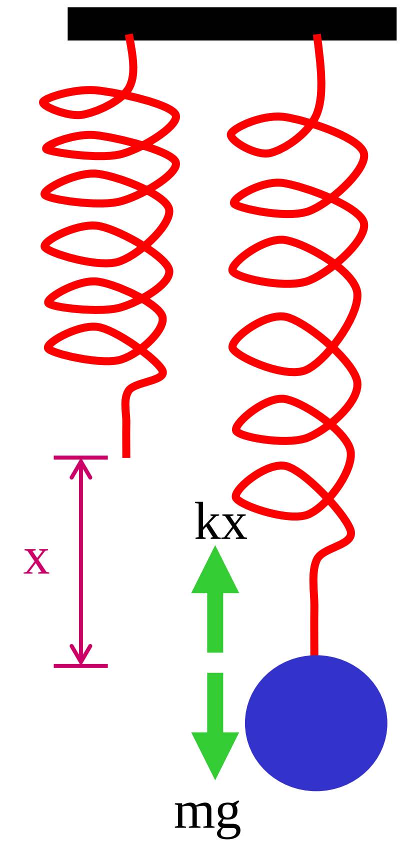
A. Less than the 3-spring system
B. The same as the 3-spring system
C. More than the 3-spring system



1. Spring constant, k = F/x.
2. This applies to each of the 3 springs, since they are being stretched **in parallel**.
3. Therefore, it takes 3X the force to stretch all 3 springs at once (***in parallel***) than it does to stretch one.

Springs: Measuring the spring constant with mass

- A spring will have an intrinsic stiffness, described by the spring constant k.
- Since $F_{applied}$ = k*x, we can determine k if we measure x and know $F_{applied}$.
- For a mass hanging from a spring, the applied force is just the force due to gravity
  - $F_{applied} = k*x = F_{gravity} = mg$
- Therefore, the spring constant will be:
  - $k = (mg)/x$

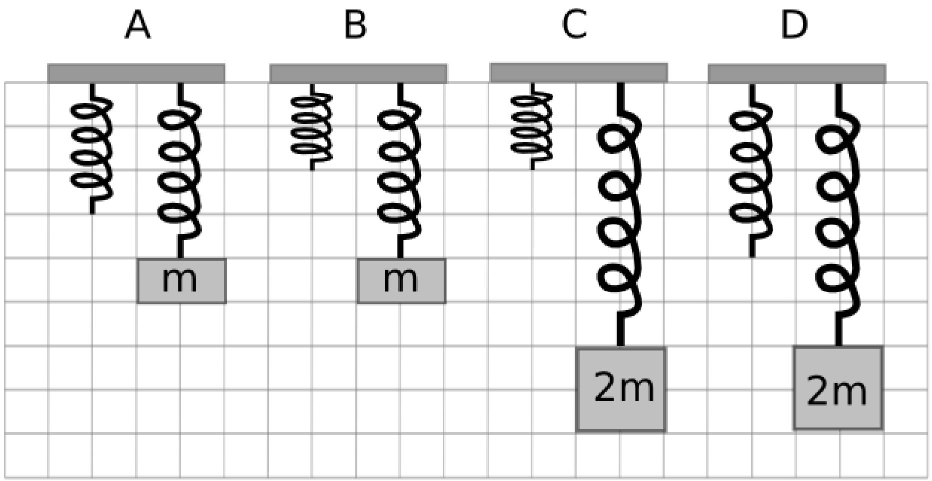


An 0.20kg mass hangs from a spring, stretching it 0.10m from its equilibrium position.
What is the spring constant of the spring?

A. 0.051 N/m
B. 0.50 N/m
C. 2.0 N/m
D. 19.6 N/m

1. $F = kx = mg$
2. $k = (mg)/x$
3. $k = \{(0.20kg)(9.8m/s^2)\}/(0.10m)$
4. $k = 19.6$ N/m

Springs A through D are shown in their unstretched positions and stretched by some hanging masses. Using the grid as a reference for displacement, rank the spring constants.



A. $k_A > k_B > k_C > k_D$

B. $k_A = k_B > k_C = k_D$

C. $k_C = k_D > k_A = k_B$

D. $k_A = k_D > k_B = k_C$

E. $k_A > k_B = k_D > k_C$

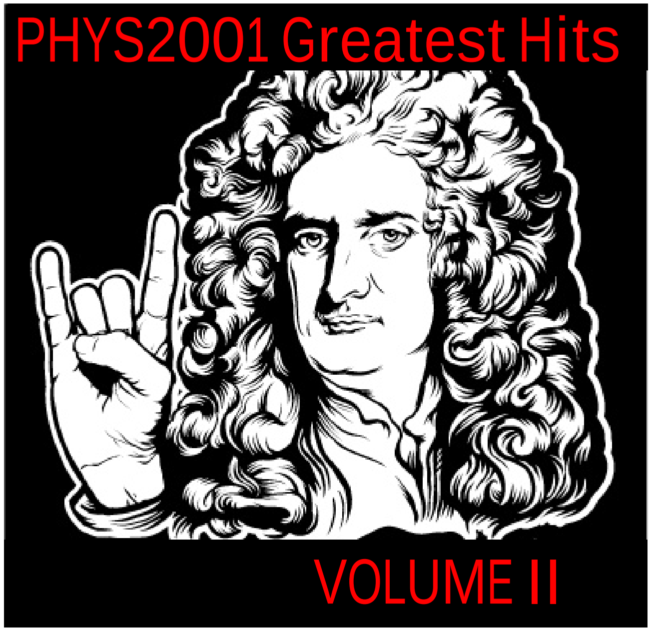
F. $k_B = k_C > k_A = k_D$

1. $F = kx = Mg$
2. $k = (Mg)/x$
3. For a fixed mass, larger displacement, x, means a smaller spring constant, k.
4. For equal displacements but larger applied mass, the spring constant must be larger.
5. Spring A stretches less than spring B for the same applied mass, so $k_A > k_B$.
6. Spring D stretches less than spring C for the same applied mass, so $k_D > k_C$.
7. M/x for A equals M/x for D and M/x for B equals M/x for C, so $k_A = k_D > k_B = k_C$.

Midterm 2 will only cover content through circular motion.

The following is a (very) brief reminder of said content.

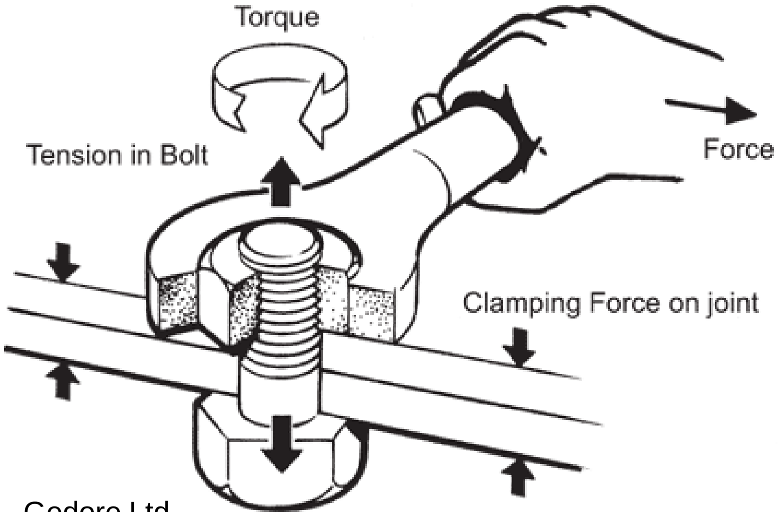
Quick review of material for midterm 2



Advice for studying:

1. Review notes
2. Try typical practice problems (a couple per topic). You can use TopHat to review problems from class.
3. Look at relevant notes section & read part of book related to problems you struggled on
4. Repeat
5. Try practice exam (& then see 1). Time yourself and grade yourself for an honest assessment.

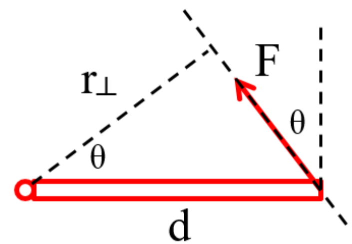
Torque:



Gedore Ltd.

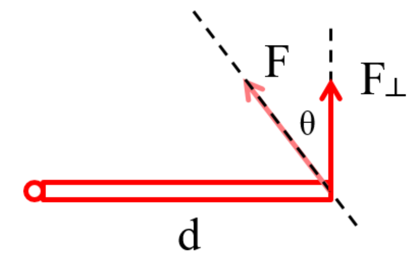
- Torque: $\tau = r \times F = |F||r|\sin(\theta)$
- Two ways to think about this:

(1) Perpendicular distance:



$\tau = F*r_\perp = F*[d*\cos(\theta)]$

(2) Perpendicular force:

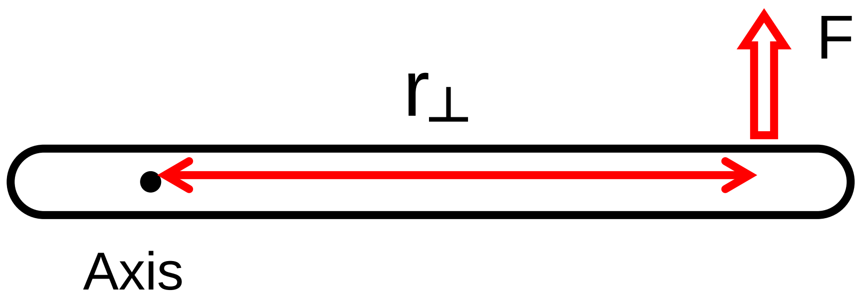


$\tau = F_\perp d = [F*\cos(\theta)]*d$

1. $F_t = m*a_t$
2. $F_t = m(r*\alpha)$
3. $(F_t*r) = m*r*r*\alpha$
4. $\tau = (m*r^2)\alpha$
5. $\tau = I*\alpha$

Torque: Force applied to a lever some perpendicular distance from an axis

- Simplest case, Force perpendicular to a lever arm:

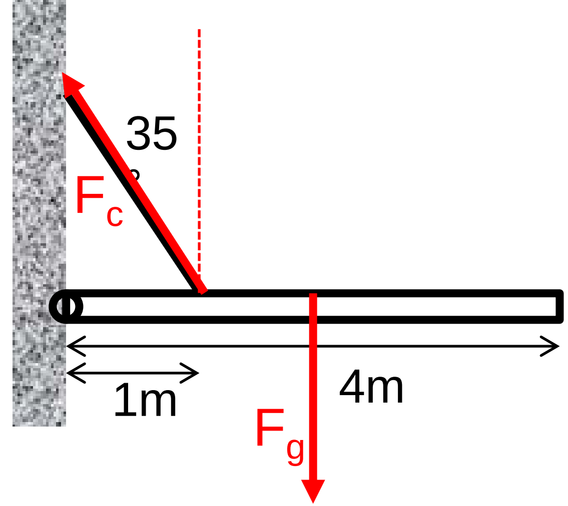


Greek letter 'tau'

- $\tau = F*r_\perp$ where $r_\perp$ is the distance from the 'axis of rotation'
  - Torque is always with respect to an axis of rotation (in fact, it's direction is along that axis of rotation). If it's a static problem, you can choose the axis of rotation.
  - Units: N*m [enter this way in LON-CAPA)

Sec. 9.2

A 1500N beam is attached to a wall by a hinge.
The beam is 4.0m long, and the mass of the beam is distributed evenly along the beam.
The beam is supported by a cable that is attached 1.0m to the beam from the wall and makes an angle of 35° from the vertical.

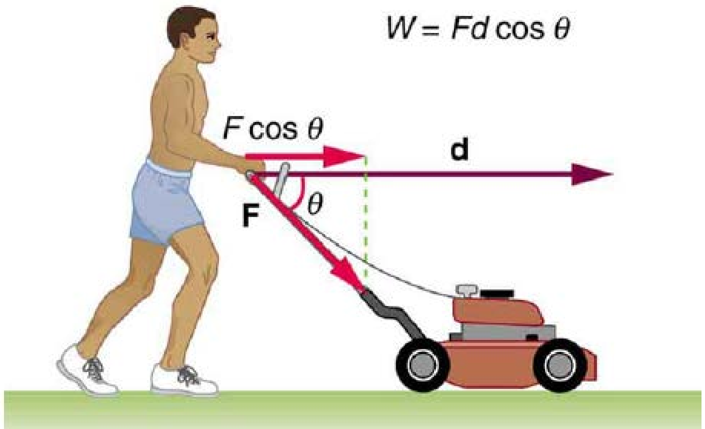


What is the tension in the cable?

(A) 1500N (B) 2460N (C) 3000 N (D) 3660 N (E) 5230 N (F) 6000N

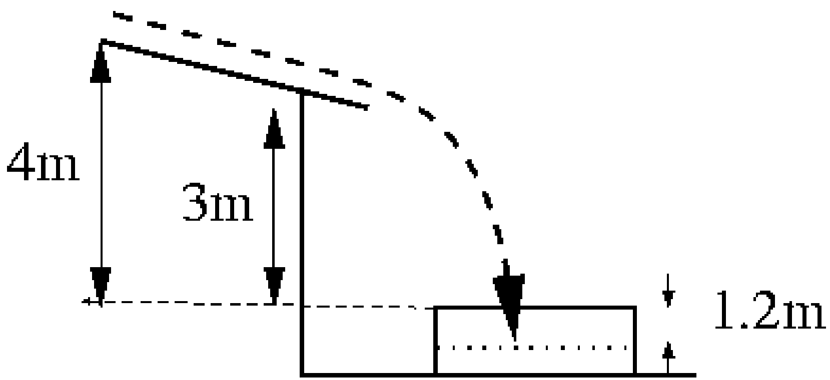
1. Choose the hinge as the axis of rotation, so that we can ignore its force, and then balance the torques about there.
2. $\sum\tau = \tau_{cable} - \tau_{gravity} = 0$
3. $\tau_{cable} = \tau_{gravity} = m_{board}g*(L_{board}/2) = (1500N)(2m) = 3000Nm$
4. $\tau_{cable} = F_{cable,\perp}r_{cable} = F_{cable}\cos(\theta)r_{cable}$
5. $F_{cable} = \tau_{cable}/[r_{cable}\cos(\theta)] = (3000Nm)/(1m*\cos(35^\circ)) \approx 3660N$

Energy



- Kinetic Energy = $KE = \frac{1}{2}mv^2$
- Potential energy = $PE = mgh$
- Work:
  - From a force: W = F*d*cos(θ)
  - From change in energy:
    - $W_{net} = KE_{final} - KE_{initial}$
    - $W_{net} = PE_{initial} - PE_{final}$
- Energy conservation:
  - $(KE_f + PE_f) = (KE_i + PE_i) + W_{NC}$
  - …***if*** $W_{NC} = 0$, then $(KE_f + PE_f) = (KE_i + PE_i)$

An 80-kg stunt-person starts at rest and slides down a roof, flies through the air, and lands on a large pad, which compresses 1.2m in order to bring the stunt-person to a stop. Assume it is an icy day and the roof is frictionless. Ignore air resistance. What is the average force on the stunt-person due to the pad?
(Hint: pick the top of the landing pad as the h=0 reference level.)



(A) 3400 N
(B) 3140 N
(C) 4080 N
(D) 0 N
(E) 940 N
(F) 2350 N

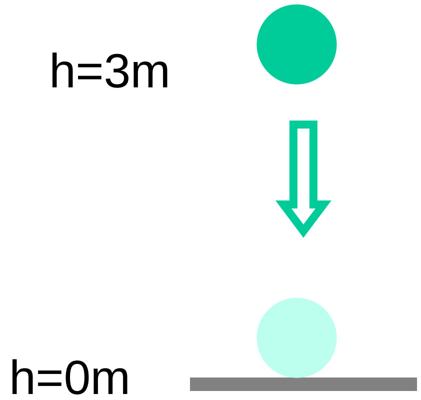
$$(KE_f + PE_f) = (KE_i + PE_i) + W_{NC}$$

1. $(KE_F + PE_F) = (KE_0 + PE_0) + W_{NC}$
2. $(0+(-1.2)mg) = (0 + 4mg) + F*d*\cos(180^o)$
3. $-1.2mg = 4mg + F*(1.2)*(-1)$
4. $1.2F = 5.2mg$
5. $F = 3400$ N

	KE	PE	E_{TOT}
Top	0	mg(4m)	4mg
Top of Pad	½mv²	0	½mv²
Rest	0	mg(-1.2m)	-1.2mg

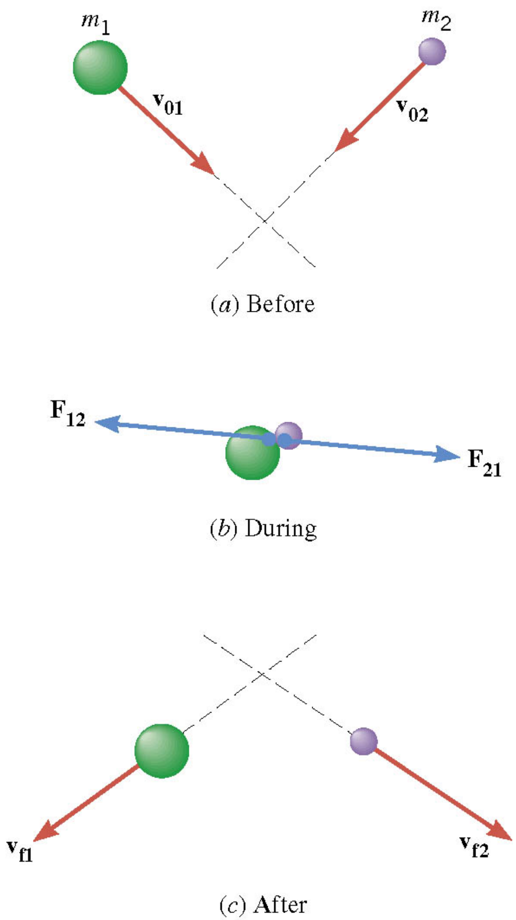
An 0.2kg ball is dropped from a height of 3.0m above the floor.
What is the speed of the ball just before it hits the floor?
(ignore air resistance)

(A) 3m/s (B) 9.8m/s (C) 5.9m/s (D) 7.7m/s



- Could use free-fall equations…
  …but using energy is easier.
- Know mass, final & initial heights, & initial velocity.
  Therefore, know:
  - $PE_i = mgh_i = (0.2kg)*(9.8m/s^2)*(3m) = 5.88J$
  - $PE_f = mgh_f = m*g*(0m) = 0J$
  - $KE_i = (1/2)mv_i^2 = (1/2)m(0m/s)^2 = 0J$
- $E_f = E_i + W_{NC}$
  - No non-conservative forces, so $W_{NC} = 0$ …. so, $E_f = E_i$
  - $PE_i + KE_i = PE_f + KE_f$
- $KE_f = 5.88J = (1/2)mv_f^2$
- $v_f = \sqrt{2KE/m} = \sqrt{2(5.88J)/(0.2kg)} = \sqrt{2(5.88kgm^2s^{-2})/(0.2kg)} = 7.7m/s$

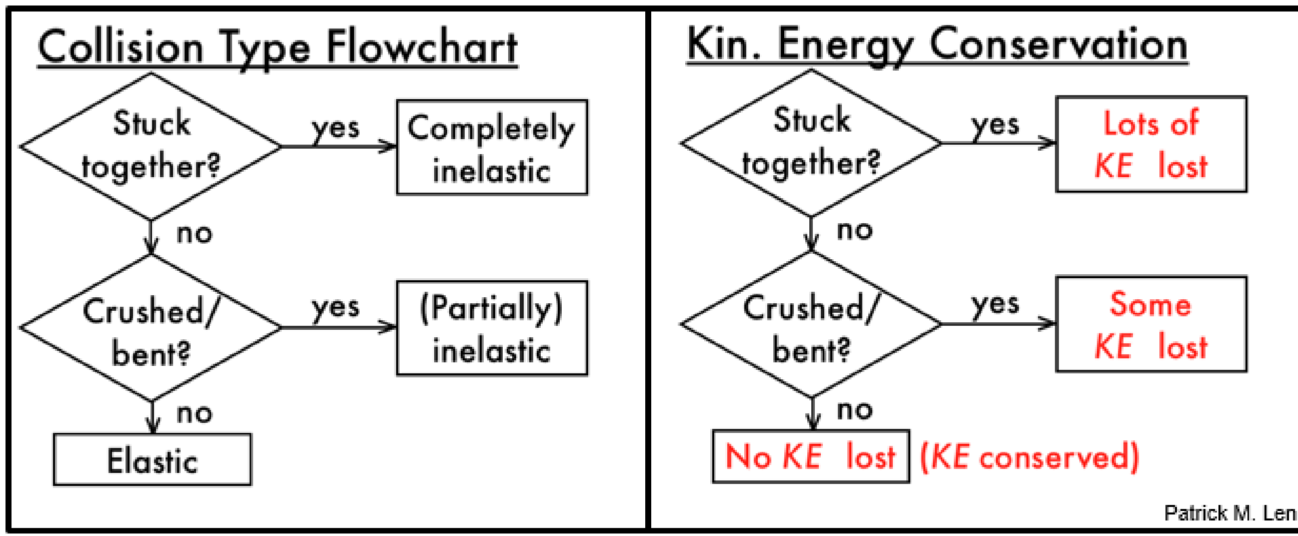
Momentum



$$m\vec{v} \quad = \vec{p}$$

Momentum is a vector and is conserved:

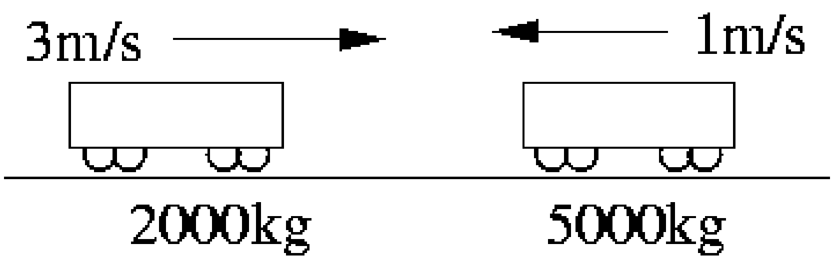
$$\sum p_{x,i} = \sum p_{x,f} \qquad \sum p_{y,i} = \sum p_{y,f}$$



$$\sum \vec{F}\Delta t = \Delta\vec{p}$$

$$\text{Impulse} = \vec{J} = \Delta\vec{p}$$

A 2000kg railroad car is traveling at 3m/s along a track.
A 5000kg railroad car is travelling on the same track,
but going in the opposite direction at 1m/s.
The two railroad cars collide and stick together.
What is the speed and direction of the smashed-together railroad cars?

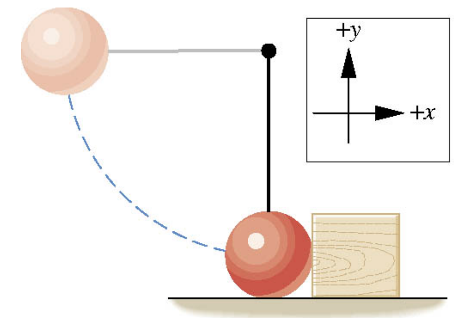


A. 0.14m/s to the right
B. 0.14m/s to the left
C. 1.6m/s to the right
D. 1.6m/s to the left
E. 7.0m/s to the right
F. 7.0m/s to the left

1. Momentum is conserved: $p_{final} = p_{initial}$
2. $p_{initial} = m_1 v_1 + m_2 v_2$ = (2000kg)(3m/s) - (5000kg)(1m/s) = 1,000kg*m/s
3. They stick together after the collision: m_{final} = 2000kg + 5000kg = 7000kg
4. $p_f = m_{final} v_{final} = p_{initial}$ = 1,000kg*m/s
5. $v_{final} = p_{final}/m_{final}$ = (1,000kg*m/s)/(7000kg) = 0.14m/s to the right

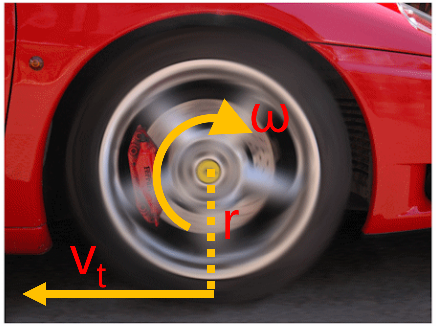
A 1.60kg ball is attached to a 1.20m-long wire,
held horizontally, and dropped.
It strikes a 2.40kg block that is sitting on a horizontal, frictionless surface.
Air resistance is negligible and the collision is elastic.
What is the velocity of the ball just before the collision?

(A) 4.33m/s (B) 18.8m/s (C) 23.5m/s **(D) 4.85m/s** (E) 3.96m/s

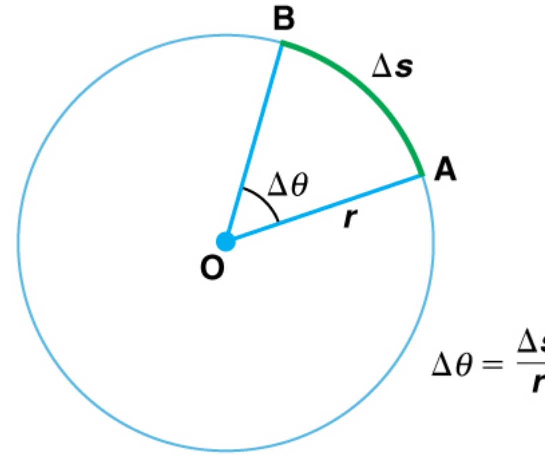


1. Total energy is conserved: $KE_i + PE_i = KE_f + PE_f$
2. Initial state: just before ball is released
    1. At rest: $KE_i = 0$.
    2. $PE_i = mgh$
3. Final: just before ball hits block
    1. At reference height h=0: $PE_f = 0$
    2. $KE_f = (1/2)mv_f^2$
4. $KE_f = (1/2)mv_f^2 = PE_i = mgh$
5. $v_f = \sqrt{\frac{2}{m}mgh} = \sqrt{2gh} = \sqrt{2(9.80\frac{m}{s^2})(1.20m)} = 4.85m/s$

Circular Motion



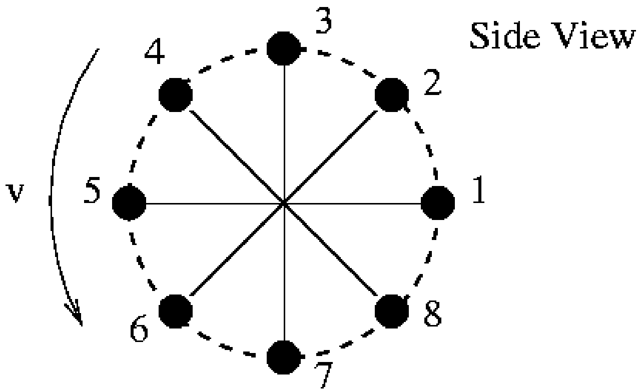
- $\theta = s/r$
- $\omega = \Delta\theta/\Delta t$
- $v_t = r*\omega$
- $\alpha = \Delta\omega/\Delta t$
- π rad = 180°
- $a_c = v_t^2/r = r*\omega^2$
- $F_c = mv^2/r$
- $F_g = G\frac{m_1 m_2}{r^2}$



Equations for kinematics in 1D & Newton's Laws apply to rotational motion as well, by subsituting the appropriate quantities:

Linear Quantity			Corresponding Rotational Quantity		
Quantity	***Variable***	***SI units***	***Quantity***	***Variable***	***SI units***
length	x	m	angle	$\theta = s/r$	rad
velocity	$v = \Delta x/\Delta t$	m/s	angular velocity	$\omega = \Delta\theta/\Delta t$	rad/s
acceleration	$a = \Delta v/\Delta t$	m/s^2	angular acceleration	$\alpha = \Delta\omega/\Delta t$	rad/s^2

You are swinging a 0.20kg tennis ball on a 1.20m-long string, where the axis of rotation is parallel to the surface of the earth.
At the minimum speed, what is the tension in the string at the bottom of the circle (position 7) ?



(A) 0.00N (B) 0.98N (C) 1.96N (D) 3.92N

1. Both gravity & the tension are supplying centripetal force.
2. Gravity is pulling outward, tension is pulling inward (in the direction of the net centripetal force).
3. $F_c = T - F_g$
4. $T = F_c + F_g = mv_t^2/r + mg$
5. $T = \{(0.20kg)(3.43m/s)^2\}/(1.2m) + (0.20kg)(9.8m/s^2)$
6. $T = 1.96N + 1.96N = 3.92N$

An 800kg car travels a distance of 20m around a turn with a radius of curvature of 40m at a speed of 25m/s in a time of 0.80s. What is the centripetal acceleration of the car?

(A) 12.5 m/s^2 (B) 15.6 m/s^2 (C) 25.0 m/s^2 (D) 12500 m/s^2

1. $a_c = v_t^2/r$
2. $a_c = \{(25m/s)^2\}/(40m)$
3. $a_c = (625\ m^2/s^2)/(40m) \approx 15.6\ m/s^2$